Syllabus

Cambridge O Level Mathematics (Syllabus D) 4024

Use this syllabus for exams in 2025, 2026 and 2027. Exams are available in the June and November series.

Version 1
Please check the syllabus page at www.cambridgeinternational.org/4024 to see if this syllabus is available in your administrative zone.

For the purposes of screen readers, any mention in this document of Cambridge IGCSE refers to Cambridge International General Certificate of Secondary Education.
Why choose Cambridge International?

Cambridge International prepares school students for life, helping them develop an informed curiosity and a lasting passion for learning. We are part of Cambridge University Press & Assessment, which is a department of the University of Cambridge.

Our Cambridge Pathway gives students a clear path for educational success from age 5 to 19. Schools can shape the curriculum around how they want students to learn – with a wide range of subjects and flexible ways to offer them. It helps students discover new abilities and a wider world, and gives them the skills they need for life, so they can achieve at school, university and work.

Our programmes and qualifications set the global standard for international education. They are created by subject experts, rooted in academic rigour and reflect the latest educational research. They provide a strong platform for learners to progress from one stage to the next, and are well supported by teaching and learning resources.

Our mission is to provide educational benefit through provision of international programmes and qualifications for school education and to be the world leader in this field. Together with schools, we develop Cambridge learners who are confident, responsible, reflective, innovative and engaged – equipped for success in the modern world.

Every year, nearly a million Cambridge students from 10,000 schools in 160 countries prepare for their future with the Cambridge Pathway.

School feedback: ‘We think the Cambridge curriculum is superb preparation for university.’
Feedback from: Christoph Guttentag, Dean of Undergraduate Admissions, Duke University, USA

Quality management
Cambridge International is committed to providing exceptional quality. In line with this commitment, our quality management system for the provision of international qualifications and education programmes for students aged 5 to 19 is independently certified as meeting the internationally recognised standard, ISO 9001:2015. Learn more at www.cambridgeinternational.org/ISO9001
Important: Changes to this syllabus

For information about changes to this syllabus for 2025, 2026 and 2027, go to page 46.
1 Why choose this syllabus?

Key benefits

Cambridge O Level is typically for 14 to 16 year olds and is an internationally recognised qualification. It has been designed especially for an international market and is sensitive to the needs of different countries. Cambridge O Level is designed for learners whose first language may not be English, and this is acknowledged throughout the examination process.

Our programmes balance a thorough knowledge and understanding of a subject and help to develop the skills learners need for their next steps in education or employment.

**Cambridge O Level Mathematics (Syllabus D)** supports learners in building competency, confidence and fluency in their use of techniques and mathematical understanding. Learners develop a feel for quantity, patterns and relationships, as well as developing reasoning, problem-solving and analytical skills in a variety of abstract and real-life contexts.

Cambridge O Level Mathematics (Syllabus D) provides a strong foundation of mathematical knowledge both for candidates studying mathematics at a higher level and those who will require mathematics to support skills in other subjects.

Our approach in Cambridge O Level Mathematics (Syllabus D) encourages learners to be:

- **confident**, in using mathematical language and techniques to ask questions, explore ideas and communicate
- **responsible**, by taking ownership of their learning, and applying their mathematical knowledge and skills so that they can reason, problem solve and work collaboratively
- **reflective**, by making connections within mathematics and across other subjects, and in evaluating methods and checking solutions
- **innovative**, by applying their knowledge and understanding to solve unfamiliar problems creatively, flexibly and efficiently
- **engaged**, by the beauty, patterns and structure of mathematics, becoming curious to learn about its many applications in society and the economy.

**School feedback:** ‘Cambridge O Level has helped me develop thinking and analytical skills which will go a long way in helping me with advanced studies.’

**Feedback from:** Kamal Khan Virk, former student at Beaconhouse Garden Town Secondary School, Pakistan, who went on to study Actuarial Science at the London School of Economics
International recognition and acceptance

Our expertise in curriculum, teaching and learning, and assessment is the basis for the recognition of our programmes and qualifications around the world. The combination of knowledge and skills in Cambridge O Level Mathematics (Syllabus D) gives learners a solid foundation for further study. Candidates who achieve grades A* to C are well prepared to follow a wide range of courses including Cambridge International AS & A Level Mathematics.

Cambridge O Levels are accepted and valued by leading universities and employers around the world as evidence of academic achievement. Many universities require a combination of Cambridge International AS & A Levels and Cambridge O Levels or equivalent to meet their entry requirements.

Learn more at www.cambridgeinternational.org/recognition
Supporting teachers

We provide a wide range of resources, detailed guidance, innovative training and professional development so that you can give your students the best possible preparation for Cambridge O Level. To find out which resources are available for each syllabus go to our School Support Hub.

The School Support Hub is our secure online site for Cambridge teachers where you can find the resources you need to deliver our programmes. You can also keep up to date with your subject and the global Cambridge community through our online discussion forums.

Find out more at www.cambridgeinternational.org/support

### Support for Cambridge O Level

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<td></td>
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<td>• Specimen papers</td>
<td>• Online forums</td>
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<td></td>
</tr>
<tr>
<td>• Syllabuses</td>
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<td></td>
</tr>
<tr>
<td>• Teacher guides</td>
<td></td>
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</tr>
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Sign up for email notifications about changes to syllabuses, including new and revised products and services at www.cambridgeinternational.org/syllabusupdates

### Professional development

We support teachers through:

- Introductory Training – face-to-face or online
- Extension Training – face-to-face or online
- Enrichment Professional Development – face-to-face or online

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- Cambridge Professional Development Qualifications

Find out more at www.cambridgeinternational.org/profdev

### Supporting exams officers

We provide comprehensive support and guidance for all Cambridge exams officers.

Find out more at: www.cambridgeinternational.org/eoguide
2 Syllabus overview

Aims

The aims describe the purposes of a course based on this syllabus.

The aims are to enable students to:

• develop a positive attitude towards mathematics in a way that encourages enjoyment, establishes confidence and promotes enquiry and further learning
• develop a feel for number and understand the significance of the results obtained
• apply their mathematical knowledge and skills to their own lives and the world around them
• use creativity and resilience to analyse and solve problems
• communicate mathematics clearly
• develop the ability to reason logically, make inferences and draw conclusions
• develop fluency so that they can appreciate the interdependence of, and connections between, different areas of mathematics
• acquire a foundation for further study in mathematics and other subjects.
Content overview

All candidates study the following topics:

1. Number
2. Algebra and graphs
3. Coordinate geometry
4. Geometry
5. Mensuration
6. Trigonometry
7. Transformations and vectors
8. Probability
9. Statistics

The subject content is organised by topic and is not presented in a teaching order. This content structure allows flexibility for teachers to plan delivery in a way that is appropriate for their learners. Learners are expected to use techniques listed in the content and apply them to solve problems with or without the use of a calculator, as appropriate.
Assessment overview

All candidates take two components. Candidates will be eligible for grades A* to E.

 Candidates should have a scientific calculator for Paper 2. Calculators are not allowed for Paper 1.

Please see the Cambridge Handbook [www.cambridgeinternational.org/eoguide](http://www.cambridgeinternational.org/eoguide) for guidance on use of calculators in the examinations.

<table>
<thead>
<tr>
<th>Paper 1: Non-calculator</th>
<th>Paper 2: Calculator</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 hours</td>
<td>2 hours</td>
</tr>
<tr>
<td>100 marks</td>
<td>100 marks</td>
</tr>
<tr>
<td>50%</td>
<td>50%</td>
</tr>
<tr>
<td>Structured and unstructured questions</td>
<td>Structured and unstructured questions</td>
</tr>
<tr>
<td>Use of a calculator is not allowed</td>
<td>A scientific calculator is required</td>
</tr>
<tr>
<td>Externally assessed</td>
<td>Externally assessed</td>
</tr>
</tbody>
</table>

Information on availability is in the Before you start section.
Assessment objectives

The assessment objectives (AOs) are:

AO1 Knowledge and understanding of mathematical techniques
Candidates should be able to:

- recall and apply mathematical knowledge and techniques
- carry out routine procedures in mathematical and everyday situations
- understand and use mathematical notation and terminology
- perform calculations with and without a calculator
- organise, process, present and understand information in written form, tables, graphs and diagrams
- estimate, approximate and work to degrees of accuracy appropriate to the context and convert between equivalent numerical forms
- understand and use measurement systems in everyday use
- measure and draw using geometrical instruments to an appropriate degree of accuracy
- recognise and use spatial relationships in two and three dimensions.

AO2 Analyse, interpret and communicate mathematically
Candidates should be able to:

- analyse a problem and identify a suitable strategy to solve it, including using a combination of processes where appropriate
- make connections between different areas of mathematics
- recognise patterns in a variety of situations and make and justify generalisations
- make logical inferences and draw conclusions from mathematical data or results
- communicate methods and results in a clear and logical form
- interpret information in different forms and change from one form of representation to another.
Weighting for assessment objectives
The approximate weightings allocated to each of the assessment objectives (AOs) are summarised below.

Assessment objectives as a percentage of the qualification

<table>
<thead>
<tr>
<th>Assessment objective</th>
<th>Weighting in O Level %</th>
</tr>
</thead>
<tbody>
<tr>
<td>AO1 Knowledge and understanding of mathematical techniques</td>
<td>40–50</td>
</tr>
<tr>
<td>AO2 Analyse, interpret and communicate mathematically</td>
<td>50–60</td>
</tr>
<tr>
<td>Total</td>
<td>100</td>
</tr>
</tbody>
</table>

Assessment objectives as a percentage of each component

<table>
<thead>
<tr>
<th>Assessment objective</th>
<th>Weighting in components %</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Paper 1</td>
</tr>
<tr>
<td>AO1 Knowledge and understanding of mathematical techniques</td>
<td>40–50</td>
</tr>
<tr>
<td>AO2 Analyse, interpret and communicate mathematically</td>
<td>50–60</td>
</tr>
<tr>
<td>Total</td>
<td>100</td>
</tr>
</tbody>
</table>
3 Subject content

This syllabus gives you the flexibility to design a course that will interest, challenge and engage your learners. Where appropriate you are responsible for selecting resources and examples to support your learners’ study. These should be appropriate for the learners’ age, cultural background and learning context as well as complying with your school policies and local legal requirements.

Learners should pursue an integrated course that allows them to fully develop their skills and understanding both with and without the use of a calculator.

A List of formulas is provided on page 2 of the examination papers for candidates to refer to during the examinations. Please note that not all required formulas are given; the ‘Notes and examples’ column of the subject content will indicate when a formula is given in the examination papers and when a formula is not given, i.e. knowledge of a formula is required.

1 Number

1.1 Types of number

<table>
<thead>
<tr>
<th>Identify and use:</th>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>• natural numbers</td>
<td>Example tasks include:</td>
</tr>
<tr>
<td>• integers (positive, zero and negative)</td>
<td>• convert between numbers and words, e.g. six billion is 6,000,000,000</td>
</tr>
<tr>
<td>• prime numbers</td>
<td>10007 is ten thousand and seven</td>
</tr>
<tr>
<td>• square numbers</td>
<td>• express 72 as a product of its prime factors</td>
</tr>
<tr>
<td>• cube numbers</td>
<td>• find the highest common factor (HCF) of two numbers</td>
</tr>
<tr>
<td>• common factors</td>
<td>• find the lowest common multiple (LCM) of two numbers.</td>
</tr>
<tr>
<td>• common multiples</td>
<td></td>
</tr>
<tr>
<td>• rational and irrational numbers</td>
<td></td>
</tr>
<tr>
<td>• reciprocals</td>
<td></td>
</tr>
</tbody>
</table>

Example tasks include:

- convert between numbers and words, e.g. six billion is 6,000,000,000
- 10007 is ten thousand and seven
- express 72 as a product of its prime factors
- find the highest common factor (HCF) of two numbers
- find the lowest common multiple (LCM) of two numbers.
1 Number (continued)

1.2 Sets

Understand and use set language, notation and Venn diagrams to describe sets and represent relationships between sets.

**Notes and examples**

Venn diagrams are limited to two or three sets. The following set notation will be used:

- \( n(A) \) Number of elements in set \( A \)
- \( \in \) ‘… is an element of …’
- \( \notin \) ‘… is not an element of …’
- \( A' \) Complement of set \( A \)
- \( \emptyset \) The empty set
- \( \mathbb{U} \) Universal set
- \( A \subseteq B \) \( A \) is a subset of \( B \)
- \( A \nsubseteq B \) \( A \) is not a subset of \( B \)
- \( A \cup B \) Union of \( A \) and \( B \)
- \( A \cap B \) Intersection of \( A \) and \( B \).

Example definition of sets:

\[ A = \{ x : x \text{ is a natural number} \} \]
\[ B = \{ (x, y) : y = mx + c \} \]
\[ C = \{ x : a \leq x \leq b \} \]
\[ D = \{ a, b, c, \ldots \} \].

1.3 Powers and roots

Calculate with the following:

- squares
- square roots
- cubes
- cube roots
- other powers and roots of numbers.

**Notes and examples**

Includes recall of squares and their corresponding roots from 1 to 15, and recall of cubes and their corresponding roots of 1, 2, 3, 4, 5, and 10, e.g.:

- Write down the value of \( \sqrt[3]{169} \).
- Work out \( 5^2 \times \sqrt[3]{8} \).
1 Number (continued)

1.4 Fractions, decimals and percentages

1 Use the language and notation of the following in appropriate contexts:
   - proper fractions
   - improper fractions
   - mixed numbers
   - decimals
   - percentages.

2 Recognise equivalence and convert between these forms.

Candidates are expected to be able to write fractions in their simplest form. Recurring decimal notation is required, e.g.

- \( 0.1\overline{7} = 0.1777… \)
- \( 0.1\overline{23} = 0.1232323… \)
- \( 0.1\overline{23} = 0.123123… \)

Includes converting between recurring decimals and fractions and vice versa, e.g. write 0.17 as a fraction.

1.5 Ordering

Order quantities by magnitude and demonstrate familiarity with the symbols =, ≠, >, <, ≥ and ≤.

1.6 The four operations

Use the four operations for calculations with integers, fractions and decimals, including correct ordering of operations and use of brackets.

Includes:
- negative numbers
- improper fractions
- mixed numbers
- practical situations, e.g. temperature changes.

1.7 Indices I

1 Understand and use indices (positive, zero, negative and fractional).

Examples include:

- \( 6^{\frac{1}{2}} = \sqrt{6} \)
- \( 16^{\frac{1}{2}} = \sqrt{16} \)

- find the value of \( 7^{-2}, 81^{\frac{1}{2}}, 8^{-\frac{1}{2}} \).

2 Understand and use the rules of indices.

E.g. find the value of \( 2^{-3} \times 2^4, (2^3)^2, 2^3 \div 2^4 \).

1.8 Standard form

1 Use the standard form \( A \times 10^n \) where \( n \) is a positive or negative integer and \( 1 \leq A < 10 \).

2 Convert numbers into and out of standard form.

3 Calculate with values in standard form.
1. **Number (continued)**

1.9 **Estimation**

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Round values to a specified degree of accuracy.</td>
</tr>
<tr>
<td>Includes decimal places and significant figures.</td>
</tr>
<tr>
<td>e.g. Write 5764 correct to the nearest thousand.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 Make estimates for calculations involving numbers, quantities and measurements.</td>
</tr>
<tr>
<td>e.g. By writing each number correct to 1 significant figure, estimate the value of $\frac{41.3}{9.79 \times 0.765}$.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 Round answers to a reasonable degree of accuracy in the context of a given problem.</td>
</tr>
</tbody>
</table>

1.10 **Limits of accuracy**

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Give upper and lower bounds for data rounded to a specified accuracy.</td>
</tr>
<tr>
<td>e.g. write down the upper bound of a length measured correct to the nearest metre.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 Find upper and lower bounds of the results of calculations which have used data rounded to a specified accuracy.</td>
</tr>
<tr>
<td>Example calculations include:</td>
</tr>
<tr>
<td>• calculate the upper bound of the perimeter or the area of a rectangle given dimensions measured to the nearest centimetre</td>
</tr>
<tr>
<td>• find the lower bound of the speed given rounded values of distance and time.</td>
</tr>
</tbody>
</table>

1.11 **Ratio and proportion**

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Understand and use ratio and proportion to:</td>
</tr>
<tr>
<td>• give ratios in their simplest form</td>
</tr>
<tr>
<td>• divide a quantity in a given ratio</td>
</tr>
<tr>
<td>• use proportional reasoning and ratios in context.</td>
</tr>
<tr>
<td>e.g. 20:30:40 in its simplest form is 2:3:4.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. adapt recipes; use map scales; determine best value.</td>
</tr>
</tbody>
</table>
## 1 Number (continued)

### 1.12 Rates

<table>
<thead>
<tr>
<th>Notes and examples</th>
<th>1 Use common measures of rate.</th>
</tr>
</thead>
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<tr>
<td>e.g. calculate with:</td>
<td>hourly rates of pay</td>
</tr>
<tr>
<td></td>
<td>exchange rates between currencies</td>
</tr>
<tr>
<td></td>
<td>flow rates</td>
</tr>
<tr>
<td></td>
<td>fuel consumption.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>2 Apply other measures of rate.</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. calculate with:</td>
</tr>
<tr>
<td>pressure</td>
</tr>
<tr>
<td>density</td>
</tr>
<tr>
<td>population density.</td>
</tr>
</tbody>
</table>

Required formulas will be given in the question.

<table>
<thead>
<tr>
<th>3 Solve problems involving average speed.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Knowledge of speed/distance/time formula is required.</td>
</tr>
<tr>
<td>e.g. A cyclist travels 45 km in 3 hours 45 minutes.</td>
</tr>
<tr>
<td>What is their average speed?</td>
</tr>
<tr>
<td>The notation used for rates will be in the form, e.g. m/s (metres per second), g/cm³ (grams per cubic centimetre).</td>
</tr>
</tbody>
</table>

### 1.13 Percentages

<table>
<thead>
<tr>
<th>Notes and examples</th>
<th>1 Calculate a given percentage of a quantity.</th>
</tr>
</thead>
</table>

| 2 Express one quantity as a percentage of another. |
| 3 Calculate percentage increase or decrease. |
| 4 Calculate with simple and compound interest. |
| 5 Calculate using reverse percentages. |
| Problems may include repeated percentage change. Formulas are not given. |
| e.g. find the cost price given the selling price and the percentage profit. |

Percentage calculations may include:
- deposit
- discount
- profit and loss (as an amount or a percentage)
- earnings
- percentages over 100%.

### 1.14 Using a calculator

<table>
<thead>
<tr>
<th>Notes and examples</th>
<th>1 Use a calculator efficiently.</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. know not to round values within a calculation and to only round the final answer.</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>2 Enter values appropriately on a calculator.</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. enter 2 hours 30 minutes as 2.5 hours or 2° 30′ 0″.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>3 Interpret the calculator display appropriately.</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. in money 4.8 means $4.80; in time 3.25 means 3 hours 15 minutes.</td>
</tr>
</tbody>
</table>
## 1 Number (continued)

### 1.15 Time

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Calculate with time: seconds (s), minutes (min), hours (h), days, weeks, months, years, including the relationship between units.</td>
</tr>
<tr>
<td>2 Calculate times in terms of the 24-hour and 12-hour clock.</td>
</tr>
<tr>
<td>3 Read clocks and timetables.</td>
</tr>
</tbody>
</table>

1 year = 365 days.

In the 24-hour clock, for example, 3.15 a.m. will be denoted by 03 15 and 3.15 p.m. by 15 15.

Includes problems involving time zones, local times and time differences.

### 1.16 Money

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Calculate with money.</td>
</tr>
<tr>
<td>2 Convert from one currency to another.</td>
</tr>
</tbody>
</table>

### 1.17 Exponential growth and decay

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Use exponential growth and decay.</td>
</tr>
</tbody>
</table>

E.g. depreciation, population change.

Knowledge of e is not required.

### 1.18 Surds

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Understand and use surds, including simplifying expressions.</td>
</tr>
<tr>
<td>2 Rationalise the denominator.</td>
</tr>
</tbody>
</table>

Examples include:

\[
\frac{10}{\sqrt{5}} = 2\sqrt{5} \\
\sqrt{200} - \sqrt{32} = 6\sqrt{2} \\
The examples include: |

\[
\frac{10}{\sqrt{5}} = 2\sqrt{5} \\
\frac{1}{-1 + \sqrt{3}} = \frac{1 + \sqrt{3}}{2}.
\]
### 2 Algebra and graphs

#### 2.1 Introduction to algebra

1. Know that letters can be used to represent generalised numbers.
2. Substitute numbers into expressions and formulas.

#### 2.2 Algebraic manipulation

1. Simplify expressions by collecting like terms.  
   Simplify means give the answer in its simplest form, e.g. \(2a^2 + 3ab - 1 + 5a^2 - 9ab + 4 = 7a^2 - 6ab + 3\).
2. Expand products of algebraic expressions.  
   e.g. expand \(3x(2x - 4y)\), \((3x + y)(x - 4y)\). Includes products of more than two brackets, e.g. expand \((x - 2)(x + 3)(2x + 1)\).
3. Factorise by extracting common factors.  
   Factorise means factorise fully, e.g. \(9x^2 + 15xy = 3x(3x + 5y)\).
4. Factorise expressions of the form:
   - \(ax + bx + kay + kby\)
   - \(a^2x^2 - b^2y^2\)
   - \(a^2 + 2ab + b^2\)
   - \(ax^2 + bx + c\)
   - \(ax^3 + bx^2 + cx\).
5. Complete the square for expressions in the form \(ax^2 + bx + c\).

#### 2.3 Algebraic fractions

1. Manipulate algebraic fractions.  
   Examples include:
   - \(\frac{x}{3} + \frac{x - 4}{2}\)
   - \(\frac{2x}{3} - \frac{3(x - 5)}{2}\)
   - \(\frac{3a}{4} \times \frac{9a}{10}\)
   - \(\frac{3a}{4} \div \frac{9a}{10}\)
   - \(\frac{1}{x - 2} + \frac{x + 1}{x - 3}\).
2. Factorise and simplify rational expressions.  
   e.g. \(\frac{x^2 - 2x}{x^2 - 5x + 6}\).
2 Algebra and graphs (continued)

2.4 Indices II

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. solve:</td>
</tr>
<tr>
<td>• $32^x = 2$</td>
</tr>
<tr>
<td>• $5^{x+1} = 25^x$</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>e.g. simplify:</th>
</tr>
</thead>
<tbody>
<tr>
<td>• $3x^{-4} \times \frac{2}{3}x^\frac{1}{2}$</td>
</tr>
<tr>
<td>• $\frac{2}{5}x^\frac{1}{2} \div 2x^{-2}$</td>
</tr>
<tr>
<td>• $\left(\frac{2x^3}{3}\right)$</td>
</tr>
</tbody>
</table>

Knowledge of logarithms is **not** required.

2.5 Equations

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. write an expression for the product of two consecutive even numbers.</td>
</tr>
<tr>
<td>Includes constructing simultaneous equations.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Examples include:</th>
</tr>
</thead>
<tbody>
<tr>
<td>• $3x + 4 = 10$</td>
</tr>
<tr>
<td>• $5 - 2x = 3(x + 7)$</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Examples include:</th>
</tr>
</thead>
<tbody>
<tr>
<td>• $\frac{x}{2x + 1} = 4$</td>
</tr>
<tr>
<td>• $\frac{2}{x + 2} + \frac{3}{2x - 1} = 1$</td>
</tr>
<tr>
<td>• $\frac{x}{x + 2} = \frac{3}{x - 6}$.</td>
</tr>
</tbody>
</table>

4 Solve simultaneous linear equations in two unknowns.

5 Solve quadratic equations by factorisation, completing the square and by use of the quadratic formula.

6 Change the subject of formulas.

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>e.g. change the subject of a formula where:</td>
</tr>
<tr>
<td>• the subject appears twice</td>
</tr>
<tr>
<td>• there is a power or root of the subject.</td>
</tr>
</tbody>
</table>
2 Algebra and graphs (continued)

2.6 Inequalities

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Represent and interpret inequalities, including on a number line.</td>
</tr>
<tr>
<td>When representing and interpreting inequalities on a number line:</td>
</tr>
<tr>
<td>• open circles should be used to represent strict inequalities (&lt;, &gt;)</td>
</tr>
<tr>
<td>• closed circles should be used to represent inclusive inequalities (≤, ≥)</td>
</tr>
<tr>
<td>e.g. –3 ≤ x &lt; 1</td>
</tr>
<tr>
<td>Example image of a number line with open and closed circles.</td>
</tr>
<tr>
<td>2 Construct, solve and interpret linear inequalities.</td>
</tr>
<tr>
<td>Examples include:</td>
</tr>
<tr>
<td>• 3x &lt; 2x + 4</td>
</tr>
<tr>
<td>• −3 ≤ 3x − 2 &lt; 7 .</td>
</tr>
<tr>
<td>3 Represent and interpret linear inequalities in two variables graphically.</td>
</tr>
<tr>
<td>The following conventions should be used:</td>
</tr>
<tr>
<td>• broken lines should be used to represent strict inequalities (&lt;, &gt;)</td>
</tr>
<tr>
<td>• solid lines should be used to represent inclusive inequalities (≤, ≥)</td>
</tr>
<tr>
<td>• shading should be used to represent unwanted regions (unless otherwise directed in the question).</td>
</tr>
<tr>
<td>e.g.</td>
</tr>
<tr>
<td>Example image of a linear inequality graph.</td>
</tr>
<tr>
<td>4 List inequalities that define a given region.</td>
</tr>
<tr>
<td>Linear programming problems are not included.</td>
</tr>
</tbody>
</table>

2.7 Sequences

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Continue a given number sequence or pattern.</td>
</tr>
<tr>
<td>Subscript notation may be used, e.g. T_n is the nth term of sequence T.</td>
</tr>
<tr>
<td>2 Recognise patterns in sequences, including the term-to-term rule, and relationships between different sequences.</td>
</tr>
<tr>
<td>Includes linear, quadratic, cubic and exponential sequences and simple combinations of these.</td>
</tr>
<tr>
<td>3 Find and use the nth term of sequences.</td>
</tr>
</tbody>
</table>
2 Algebra and graphs (continued)

2.8 Proportion

Express direct and inverse proportion in algebraic terms and use this form of expression to find unknown quantities.

Includes linear, square, square root, cube and cube root proportion. Knowledge of proportional symbol (∝) is required.

2.9 Graphs in practical situations

1. Use and interpret graphs in practical situations including travel graphs and conversion graphs.

Includes estimation and interpretation of the gradient of a tangent at a point.

2. Draw graphs from given data.

3. Apply the idea of rate of change to simple kinematics involving distance–time and speed–time graphs, acceleration and deceleration.

Areas will involve linear sections only.

4. Calculate distance travelled as area under a speed–time graph.

2.10 Graphs of functions

1. Construct tables of values, and draw, recognise and interpret graphs for functions of the following forms:
   - \( ax^n \) (includes sums of no more than three of these)
   - \( ab^x + c \)
     where \( n = -2, -1, -\frac{1}{2}, 0, \frac{1}{2}, 1, 2, 3; \) \( a \) and \( c \) are rational numbers; and \( b \) is a positive integer.

Examples include:
   - \( y = x^3 + x - 4 \)
   - \( y = 2x + \frac{3}{x^2} \)
   - \( y = \frac{1}{4} \times 2^x \).

2. Solve associated equations graphically, including finding and interpreting roots by graphical methods.

E.g. finding the intersection of a line and a curve.

3. Draw and interpret graphs representing exponential growth and decay problems.

4. Estimate gradients of curves by drawing tangents.
2 Algebra and graphs (continued)

2.11 Sketching curves

Recognise, sketch and interpret graphs of the following functions:

(a) linear
(b) quadratic
(c) cubic
(d) reciprocal
(e) exponential.

Notes and examples

Where \( a, b, c, \) and \( d \) are rational numbers, functions will be equivalent to:

- \( ax + by = c \)
- \( y = ax^2 + bx + c \)
- \( y = ax^3 + d \)
- \( y = ax^3 + bx^2 + cx \).

Where \( m \) and \( n \) are integers, functions will be equivalent to:

- \( y = \frac{m}{x} + n \)
- \( y = mx^2 + n \).

Knowledge of turning points, vertical and horizontal asymptotes, roots and symmetry is required.

Finding turning points of quadratics by completing the square may be required.

2.12 Functions

1. Understand functions, domain and range, and use function notation.

Examples include:

- \( f(x) = 3x - 5 \)
- \( g(x) = \frac{3(x + 4)}{5} \)
- \( h(x) = 2x^2 + 3 \).

2. Understand and find inverse functions \( f^{-1}(x) \).

3. Form composite functions as defined by \( g(f(x)) = g(f(x)) \).

E.g. \( f(x) = \frac{3}{x + 2} \) and \( g(x) = (3x + 5)^2 \). Find \( fg(x) \).

Give your answer as a fraction in its simplest form.

Candidates are not expected to find the domains and ranges of composite functions.

This topic may include mapping diagrams.
## 3 Coordinate geometry

### 3.1 Coordinates

Use and interpret Cartesian coordinates in two dimensions.

### 3.2 Drawing linear graphs

Draw straight-line graphs for linear equations.

Examples include:
- \( y = -2x + 5 \)
- \( y = 7 - 4x \)
- \( 3x + 2y = 5 \)

### 3.3 Gradient of linear graphs

1. Find the gradient of a straight line.
2. Calculate the gradient of a straight line from the coordinates of two points on it.

### 3.4 Length and midpoint

1. Calculate the length of a line segment.
2. Find the coordinates of the midpoint of a line segment.

### 3.5 Equations of linear graphs

Interpret and obtain the equation of a straight-line graph.

Questions may:
- use and request lines in different forms, e.g. 
  - \( ax + by = c \)
  - \( y = mx + c \)
  - \( x = k \)
- involve finding the equation when the graph is given
- ask for the gradient or \( y \)-intercept of a graph from an equation, e.g. find the gradient and \( y \)-intercept of the graph with equation \( 5x + 4y = 8 \).

Candidates are expected to give equations of a line in a fully simplified form.
### Coordinate geometry (continued)

<table>
<thead>
<tr>
<th>3.6 Parallel lines</th>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Find the gradient and equation of a straight line parallel to a given line.</td>
<td>e.g. Find the equation of the line parallel to $y = 4x - 1$ that passes through $(1, -3)$.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>3.7 Perpendicular lines</th>
<th>Notes and examples</th>
</tr>
</thead>
</table>
| Find the gradient and equation of a straight line perpendicular to a given line. | Examples include:  
  - Find the gradient of a line perpendicular to $2y = 3x + 1$.  
  - Find the equation of the perpendicular bisector of the line joining the points $(-3, 8)$ and $(9, -2)$. |
# 4 Geometry

## 4.1 Geometrical terms

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Candidates are <strong>not</strong> expected to show that two shapes are congruent.</td>
</tr>
</tbody>
</table>

### 1 Use and interpret the following geometrical terms:
- point
- vertex
- line
- plane
- parallel
- perpendicular
- perpendicular bisector
- bearing
- right angle
- acute, obtuse and reflex angles
- interior and exterior angles
- similar
- congruent
- scale factor.

### 2 Use and interpret the vocabulary of:
- triangles
- special quadrilaterals
- polygons
- nets
- solids.

Includes the following terms.

**Triangles:**
- equilateral
- isosceles
- scalene
- right-angled.

**Quadrilaterals:**
- square
- rectangle
- kite
- rhombus
- parallelogram
- trapezium.

*continued*
4 Geometry (continued)

4.1 Geometrical terms (continued)  Notes and examples

Polygons:
- regular and irregular polygons
- pentagon
- hexagon
- octagon
- decagon.

Solids:
- cube
- cuboid
- prism
- cylinder
- pyramid
- cone
- sphere
- hemisphere
- frustum
- face
- surface
- edge.

3 Use and interpret the vocabulary of a circle.

Includes the following terms:
- centre
- radius (plural radii)
- diameter
- circumference
- semicircle
- chord
- tangent
- major and minor arc
- sector
- segment.
### 4 Geometry (continued)

#### 4.2 Geometrical constructions

<table>
<thead>
<tr>
<th></th>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Measure and draw lines and angles.</td>
</tr>
<tr>
<td>2</td>
<td>Construct a triangle, given the lengths of all sides, using a ruler and pair of compasses only.</td>
</tr>
<tr>
<td>3</td>
<td>Draw, use and interpret nets.</td>
</tr>
</tbody>
</table>

A ruler should be used for all straight edges. Constructions of perpendicular bisectors and angle bisectors are **not** required.

Examples include:
- draw nets of cubes, cuboids, prisms and pyramids
- use measurements from nets to calculate volumes and surface areas.

#### 4.3 Scale drawings

<table>
<thead>
<tr>
<th></th>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Draw and interpret scale drawings.</td>
</tr>
<tr>
<td>2</td>
<td>Use and interpret three-figure bearings.</td>
</tr>
</tbody>
</table>

A ruler must be used for all straight edges. Bearings are measured clockwise from north (000° to 360°), e.g. Find the bearing of A from B if the bearing of B from A is 025°.

Includes an understanding of the terms north, east, south and west, e.g. point D is due east of point C.

#### 4.4 Similarity

<table>
<thead>
<tr>
<th></th>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Calculate lengths of similar shapes.</td>
</tr>
<tr>
<td>2</td>
<td>Use the relationships between lengths and areas of similar shapes and lengths, surface areas and volumes of similar solids.</td>
</tr>
<tr>
<td>3</td>
<td>Solve problems and give simple explanations involving similarity.</td>
</tr>
</tbody>
</table>

Includes use of scale factor, e.g.

\[
\frac{\text{Volume of } A}{\text{Volume of } B} = \left(\frac{\text{Length of } A}{\text{Length of } B}\right)^3
\]

Includes showing that two triangles are similar using geometric reasons.

#### 4.5 Symmetry

<table>
<thead>
<tr>
<th></th>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Recognise line symmetry and order of rotational symmetry in two dimensions.</td>
</tr>
<tr>
<td>2</td>
<td>Recognise symmetry properties of prisms, cylinders, pyramids and cones.</td>
</tr>
</tbody>
</table>

Includes properties of triangles, quadrilaterals and polygons directly related to their symmetries.

e.g. identify planes and axes of symmetry.
### 4 Geometry (continued)

#### 4.6 Angles

1. Calculate unknown angles and give simple explanations using the following geometrical properties:
   - sum of angles at a point = 360°
   - sum of angles at a point on a straight line = 180°
   - vertically opposite angles are equal
   - angle sum of a triangle = 180° and angle sum of a quadrilateral = 360°.

2. Calculate unknown angles and give geometric explanations for angles formed within parallel lines:
   - corresponding angles are equal
   - alternate angles are equal
   - co-interior (supplementary) angles sum to 180°.

3. Know and use angle properties of regular and irregular polygons.

   Knowledge of three-letter notation for angles is required, e.g. angle $ABC$. Candidates are expected to use the correct geometrical terminology when giving reasons for answers.

#### 4.7 Circle theorems I

Calculate unknown angles and give explanations using the following geometrical properties of circles:

- angle in a semicircle = 90°
- angle between tangent and radius = 90°
- angle at the centre is twice the angle at the circumference
- angles in the same segment are equal
- opposite angles of a cyclic quadrilateral sum to 180° (supplementary)
- alternate segment theorem.

Candidates are expected to use the geometrical properties listed in the syllabus when giving reasons for answers.

#### 4.8 Circle theorems II

Use the following symmetry properties of circles:

- equal chords are equidistant from the centre
- the perpendicular bisector of a chord passes through the centre
- tangents from an external point are equal in length.

Candidates will be expected to use the geometrical properties listed in the syllabus when giving reasons for answers.
5 Mensuration

5.1 Units of measure

Use metric units of mass, length, area, volume and capacity in practical situations and convert quantities into larger or smaller units.

Units include:
• mm, cm, m, km
• mm², cm², m², km²
• mm³, cm³, m³
• ml, l
• g, kg .

Conversion between units includes:
• between different units of area, e.g. cm² ↔ m²
• between units of volume and capacity, e.g. m³ ↔ litres.

5.2 Area and perimeter

Carry out calculations involving the perimeter and area of a rectangle, triangle, parallelogram and trapezium.

Except for the area of a triangle, formulas are not given.

5.3 Circles, arcs and sectors

1 Carry out calculations involving the circumference and area of a circle.
2 Carry out calculations involving arc length and sector area as fractions of the circumference and area of a circle.

Answers may be asked for in terms of $\pi$. Formulas are given in the List of formulas. Includes minor and major sectors.

5.4 Surface area and volume

Carry out calculations and solve problems involving the surface area and volume of a:
• cuboid
• prism
• cylinder
• sphere
• pyramid
• cone.

Answers may be asked for in terms of $\pi$. The following formulas are given in the List of formulas:
• curved surface area of a cylinder
• curved surface area of a cone
• surface area of a sphere
• volume of a prism
• volume of a pyramid
• volume of a cylinder
• volume of a cone
• volume of a sphere.
## 5 Mensuration (continued)

### 5.5 Compound shapes and parts of shapes

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Carry out calculations and solve problems involving perimeters and areas of:</td>
</tr>
<tr>
<td>• compound shapes</td>
</tr>
<tr>
<td>• parts of shapes.</td>
</tr>
<tr>
<td>2 Carry out calculations and solve problems involving surface areas and volumes of:</td>
</tr>
<tr>
<td>• compound solids</td>
</tr>
<tr>
<td>• parts of solids.</td>
</tr>
</tbody>
</table>

Answers may be asked for in terms of $\pi$.  
E.g. find the surface area and volume of a frustum.
6 Trigonometry

6.1 Pythagoras’ theorem

Know and use Pythagoras’ theorem.

6.2 Right-angled triangles

1 Know and use the sine, cosine and tangent ratios for acute angles in calculations involving sides and angles of a right-angled triangle.

2 Solve problems in two dimensions using Pythagoras’ theorem and trigonometry.

3 Know that the perpendicular distance from a point to a line is the shortest distance to the line.

4 Carry out calculations involving angles of elevation and depression.

Angles will be given in degrees and answers should be written in degrees, with decimals correct to one decimal place.

Knowledge of bearings may be required.

6.3 Non-right-angled triangles

1 Use the sine and cosine rules in calculations involving lengths and angles for any triangle.

2 Use the formula area of triangle = $\frac{1}{2}ab\sin C$.

Includes problems involving obtuse angles and the ambiguous case.

The sine and cosine rules and the formula for area of a triangle are given in the List of formulas.

6.4 Pythagoras’ theorem and trigonometry in 3D

Carry out calculations and solve problems in three dimensions using Pythagoras’ theorem and trigonometry, including calculating the angle between a line and a plane.
7 Transformations and vectors

7.1 Transformations

Recognise, describe and draw the following transformations:

1. Reflection of a shape in a straight line.
2. Rotation of a shape about a centre through multiples of 90°.
3. Enlargement of a shape from a centre by a scale factor.
4. Translation of a shape by a vector \( \begin{pmatrix} x \\ y \end{pmatrix} \).

Questions may involve combinations of transformations. A ruler must be used for all straight edges.

Positive, fractional and negative scale factors may be used.

7.2 Vectors in two dimensions

1. Describe a translation using a vector represented by \( \begin{pmatrix} x \\ y \end{pmatrix} \), \( \overrightarrow{AB} \) or \( \mathbf{a} \).
2. Add and subtract vectors.
3. Multiply a vector by a scalar.

Vectors will be printed as \( \overrightarrow{AB} \) or \( \mathbf{a} \).

7.3 Magnitude of a vector

Calculate the magnitude of a vector \( \begin{pmatrix} x \\ y \end{pmatrix} \) as \( \sqrt{x^2 + y^2} \) as

The magnitudes of vectors will be denoted by modulus signs, e.g.

- \( |\mathbf{a}| \) is the magnitude of \( \mathbf{a} \)
- \( |\overrightarrow{AB}| \) is the magnitude of \( \overrightarrow{AB} \).

7.4 Vector geometry

1. Represent vectors by directed line segments.
2. Use position vectors.
3. Use the sum and difference of two or more vectors to express given vectors in terms of two coplanar vectors.
4. Use vectors to reason and to solve geometric problems.

Examples include:

- show that vectors are parallel
- show that 3 points are collinear
- solve vector problems involving ratio and similarity.
8 **Probability**

### 8.1 Introduction to probability

1. Understand and use the probability scale from 0 to 1.

2. Understand and use probability notation. P(\(A\)) is the probability of \(A\).
   P(\(A'\)) is the probability of not \(A\).

3. Calculate the probability of a single event. Probabilities should be given as a fraction, decimal or percentage.
   Problems may require using information from tables, graphs or Venn diagrams.

4. Understand that the probability of an event not occurring = 1 – the probability of the event occurring.
   e.g. \(P(B) = 0.8\), find \(P(B')\).

### 8.2 Relative and expected frequencies

1. Understand relative frequency as an estimate of probability.
   e.g. use results of experiments with a spinner to estimate the probability of a given outcome.

2. Calculate expected frequencies.
   e.g. use probability to estimate an expected value from a population.
   Includes understanding what is meant by fair and bias.

### 8.3 Probability of combined events

Calculate the probability of combined events using, where appropriate:
- sample space diagrams
- Venn diagrams
- tree diagrams.

Combined events could be with or without replacement.

The notation \(P(A \cap B)\) and \(P(A \cup B)\) may be used in the context of Venn diagrams.

On tree diagrams outcomes will be written at the end of the branches and probabilities by the side of the branches.
## 9 Statistics

### 9.1 Classifying statistical data
Classify and tabulate statistical data.

- e.g. tally tables, two-way tables.

### 9.2 Interpreting statistical data
1. Read, interpret and draw inferences from tables and statistical diagrams.
2. Compare sets of data using tables, graphs and statistical measures.
3. Appreciate restrictions on drawing conclusions from given data.

- e.g. compare averages and measures of spread between two data sets.

### 9.3 Averages and measures of spread
1. Calculate the mean, median, mode and range for individual data and distinguish between the purposes for which these are used.
2. Calculate an estimate of the mean for grouped discrete or grouped continuous data.
3. Identify the modal class from a grouped frequency distribution.

### 9.4 Statistical charts and diagrams
Draw and interpret:

(a) bar charts
(b) pie charts
(c) pictograms
(d) simple frequency distributions.

- Includes composite (stacked) and dual (side-by-side) bar charts.
### 9 Statistics (continued)

#### 9.5 Scatter diagrams

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Draw and interpret scatter diagrams.</td>
</tr>
<tr>
<td>Plotted points should be clearly marked, for example as small crosses (×).</td>
</tr>
<tr>
<td>Understand what is meant by positive, negative and zero correlation.</td>
</tr>
<tr>
<td>A line of best fit:</td>
</tr>
<tr>
<td>• should be a single ruled line drawn by inspection</td>
</tr>
<tr>
<td>• should extend across the full data set</td>
</tr>
<tr>
<td>• does not need to coincide exactly with any of the points but there should be a roughly even distribution of points either side of the line over its entire length.</td>
</tr>
<tr>
<td>Draw by eye, interpret and use a straight line of best fit.</td>
</tr>
</tbody>
</table>

#### 9.6 Cumulative frequency diagrams

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Draw and interpret cumulative frequency tables and diagrams.</td>
</tr>
<tr>
<td>Plotted points on a cumulative frequency diagram should be clearly marked, for example as small crosses (×), and be joined with a smooth curve.</td>
</tr>
<tr>
<td>Estimate and interpret the median, percentiles, quartiles and interquartile range from cumulative frequency diagrams.</td>
</tr>
</tbody>
</table>

#### 9.7 Histograms

<table>
<thead>
<tr>
<th>Notes and examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Draw and interpret histograms.</td>
</tr>
<tr>
<td>On histograms, the vertical axis is labelled ‘Frequency density’.</td>
</tr>
<tr>
<td>Calculate with frequency density.</td>
</tr>
<tr>
<td>Frequency density is defined as frequency density = frequency ÷ class width.</td>
</tr>
</tbody>
</table>
4 Details of the assessment

All candidates take two components. Candidates will be eligible for grades A* to E.

Both papers assess AO1 Knowledge and understanding of mathematical techniques and AO2 Analyse, interpret and communicate mathematically.

Both papers consist of structured and unstructured questions. Structured questions contain parts, e.g. (a), (b), (c)(i), etc., and unstructured questions do not.

Questions may assess more than one topic from the subject content.

For all papers, candidates write their answers on the question paper. They must show all necessary working in the spaces provided.

Additional materials for exams

For both papers, candidates should have the following geometrical instruments:
- a pair of compasses
- a protractor
- a ruler.

Tracing paper may be used as an additional material for all papers. Candidates cannot bring their own tracing paper but may request it during the examination.

Candidates should have a scientific calculator for Paper 2; one with trigonometric functions is strongly recommended. Algebraic or graphical calculators are not permitted. Please see the Cambridge Handbook www.cambridgeinternational.org/eoguide for guidance on use of calculators in the examinations. Calculators are not allowed for Paper 1.

The Additional materials list for exams is updated before each series. You can view the list for the relevant series and year on our website in the Phase 4 – Before the exams section of the Cambridge Exams Officer’s Guide www.cambridgeinternational.org/eoguide

Paper 1 Non-calculator

Written paper, 2 hours, 100 marks.
Use of a calculator is not allowed.
Candidates answer all questions.
This paper consists of questions based on any of the subject content, except for 1.14 Using a calculator.
This paper will be weighted at 50% of the total qualification.
This written paper is an externally set assessment, marked by Cambridge.
Paper 2 Calculator

Written paper, 2 hours, 100 marks.
A scientific calculator is required.
Candidates answer all questions.
This paper consists of questions based on any of the subject content.

Candidates should give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

To earn accuracy marks, candidates should avoid rounding figures until they have their final answer. Where candidates need to use a final answer in later parts of the question, they should use the value of the final answer before it was rounded.

Candidates should use the value of π from their calculator or the value of 3.142.
This paper will be weighted at 50% of the total qualification.
This written paper is an externally set assessment, marked by Cambridge.
**List of formulas**

This list of formulas will be included on page 2 of the examination papers.

Area, $A$, of triangle, base $b$, height $h$.  
\[ A = \frac{1}{2}bh \]

Area, $A$, of circle of radius $r$.  
\[ A = \pi r^2 \]

Circumference, $C$, of circle of radius $r$.  
\[ C = 2\pi r \]

Curved surface area, $A$, of cylinder of radius $r$, height $h$.  
\[ A = 2\pi rh \]

Curved surface area, $A$, of cone of radius $r$, sloping edge $l$.  
\[ A = \pi rl \]

Surface area, $A$, of sphere of radius $r$.  
\[ A = 4\pi r^2 \]

Volume, $V$, of prism, cross-sectional area $A$, length $l$.  
\[ V = Al \]

Volume, $V$, of pyramid, base area $A$, height $h$.  
\[ V = \frac{1}{3}Ah \]

Volume, $V$, of cylinder of radius $r$, height $h$.  
\[ V = \pi r^2h \]

Volume, $V$, of cone of radius $r$, height $h$.  
\[ V = \frac{1}{3}\pi r^2h \]

Volume, $V$, of sphere of radius $r$.  
\[ V = \frac{4}{3}\pi r^3 \]

For the equation, $ax^2 + bx + c = 0$, where $a \neq 0$  
\[ x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \]

For the triangle shown,

\[
\begin{align*}
\frac{a}{\sin A} &= \frac{b}{\sin B} = \frac{c}{\sin C} \\
a^2 &= b^2 + c^2 - 2bc \cos A \\
\text{Area} &= \frac{1}{2}ab \sin C
\end{align*}
\]
Mathematical conventions

Mathematics is a universal language where there are some similarities and differences around the world. The guidance below outlines the conventions used in Cambridge examinations and we encourage candidates to follow these conventions.

Working with graphs

- **A plot** of a graph should have points clearly marked, for example as small crosses (×), and **must**:
  - be drawn on graph or squared paper
  - cover a given range of values by calculating the coordinates of points and connecting them appropriately (where values are given, it will include enough points to determine a curve; where a table of values is not provided, the candidate must decide on the appropriate number of points required to determine the curve)
  - have each point plotted to an accuracy of within half of the smallest square on the grid.

- **A sketch** of a graph does not have to be accurate or to scale, nor does it need to be on graph or squared paper, but it **must**:
  - be drawn freehand
  - show the most important features, e.g. x-intercepts, y-intercepts, turning points, symmetry, with coordinates or values marked on the axes, where appropriate
  - have labelled axes, e.g. with x and y
  - interact with the axes appropriately, e.g. by intersecting or by tending towards
  - fall within the correct quadrants
  - show the correct long-term behaviour.

- Graphs should extend as far as possible across any given grid, within any constraints of the domain.

- Where graphs of functions are:
  - linear, they should be ruled.
  - non-linear, the points should be joined with a smooth curve.

- A tangent to a curve should touch the curve at the required point and be in contact with the curve for the minimum possible distance. It should not cross the curve at the point where it is a tangent.

- Values should be read off a graph to an accuracy of within half of the smallest square on the grid.

Communicating mathematically

- If candidates are asked to show their working, they cannot gain full marks without clearly communicating their method, even if their final answer is correct.

- A numerical answer should not be given as a combination of fractions and decimals, e.g. \( \frac{1}{0.2} \) is **not** acceptable.
Accuracy

- Answers are expected to be given in their simplest form unless the question states otherwise.
- Where a question asks for ‘exact values’ the answer may need to be given in terms of \( \pi \) or in surd form, depending on the question.
- Where answers are not exact values, they should be given to 3 significant figures unless a different accuracy is defined in the question.
- Answers that are exact to 4 or 5 significant figures should not be rounded unless the question states otherwise.
- In order to obtain an answer correct to an appropriate degree of accuracy, a higher degree of accuracy will often be needed within the working.
- If a question asks to prove or show a given answer to a specified degree of accuracy, candidates must show full working, intermediate answers and the final answer to at least one degree of accuracy more than that asked for.
### Command words

Command words and their meanings help candidates know what is expected from them in the exams. The table below includes command words used in the assessment for this syllabus. The use of the command word will relate to the subject context.

<table>
<thead>
<tr>
<th>Command word</th>
<th>What it means</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calculate</td>
<td>work out from given facts, figures or information</td>
</tr>
<tr>
<td>Construct</td>
<td>make an accurate drawing</td>
</tr>
<tr>
<td>Determine</td>
<td>establish with certainty</td>
</tr>
<tr>
<td>Describe</td>
<td>state the points of a topic / give characteristics and main features</td>
</tr>
<tr>
<td>Explain</td>
<td>set out purposes or reasons / make the relationships between things clear / say why and/or how and support with relevant evidence</td>
</tr>
<tr>
<td>Give</td>
<td>produce an answer from a given source or recall/memory</td>
</tr>
<tr>
<td>Plot</td>
<td>mark point(s) on a graph</td>
</tr>
<tr>
<td>Show (that)</td>
<td>provide structured evidence that leads to a given result</td>
</tr>
<tr>
<td>Sketch</td>
<td>make a simple freehand drawing showing the key features</td>
</tr>
<tr>
<td>State</td>
<td>express in clear terms</td>
</tr>
<tr>
<td>Work out</td>
<td>calculate from given facts, figures or information with or without the use of a calculator</td>
</tr>
<tr>
<td>Write</td>
<td>give an answer in a specific form</td>
</tr>
<tr>
<td>Write down</td>
<td>give an answer without significant working</td>
</tr>
</tbody>
</table>
5 What else you need to know

This section is an overview of other information you need to know about this syllabus. It will help to share the administrative information with your exams officer so they know when you will need their support. Find more information about our administrative processes at www.cambridgeinternational.org/eoguide

Before you start

Previous study

We recommend that learners starting this course should have studied a mathematics curriculum such as the Cambridge Lower Secondary programme or equivalent national educational framework.

Guided learning hours

We design Cambridge O Level syllabuses to require about 130 guided learning hours for each subject. This is for guidance only. The number of hours a learner needs to achieve the qualification may vary according to each school and the learners’ previous experience of the subject.

Availability and timetables

All Cambridge schools are allocated to one of six administrative zones. Each zone has a specific timetable. Cambridge O Levels are available to centres in administrative zones 3, 4 and 5.

You can enter candidates in the June and November exam series. You can view the timetable for your administrative zone at www.cambridgeinternational.org/timetables

Check you are using the syllabus for the year the candidate is taking the exam.

Private candidates can enter for this syllabus. For more information, please refer to the Cambridge Guide to Making Entries.

Combining with other syllabuses

Candidates can take this syllabus alongside other Cambridge International syllabuses in a single exam series. The only exceptions are:

- Cambridge IGCSE Mathematics 0580
- Cambridge IGCSE (9–1) Mathematics 0980
- Cambridge IGCSE International Mathematics 0607
- syllabuses with the same title at the same level.

Cambridge O Level, Cambridge IGCSE™ and Cambridge IGCSE (9–1) syllabuses are at the same level.
Making entries
Exams officers are responsible for submitting entries to Cambridge International. We encourage them to work closely with you to make sure they enter the right number of candidates for the right combination of syllabus components. Entry option codes and instructions for submitting entries are in the Cambridge Guide to Making Entries. Your exams officer has a copy of this guide.

Exam administration
To keep our exams secure, we produce question papers for different areas of the world, known as administrative zones. We allocate all Cambridge schools to an administrative zone determined by their location. Each zone has a specific timetable. Some of our syllabuses offer candidates different assessment options. An entry option code is used to identify the components the candidate will take relevant to the administrative zone and the available assessment options.

Support for exams officers
We know how important exams officers are to the successful running of exams. We provide them with the support they need to make your entries on time. Your exams officer will find this support, and guidance for all other phases of the Cambridge Exams Cycle, at www.cambridgeinternational.org/eoguide

Retakes
Candidates can retake the whole qualification as many times as they want to. Information on retake entries is at www.cambridgeinternational.org/retakes

Language
This syllabus and the related assessment materials are available in English only.

Accessibility and equality
Syllabus and assessment design
Cambridge International works to avoid direct or indirect discrimination. We develop and design syllabuses and assessment materials to maximise inclusivity for candidates of all national, cultural or social backgrounds and candidates with protected characteristics; these protected characteristics include special educational needs and disability, religion and belief, and characteristics related to gender and identity. In addition, the language and layout used are designed to make our materials as accessible as possible. This gives all candidates the fairest possible opportunity to demonstrate their knowledge, skills and understanding and helps to minimise the requirement to make reasonable adjustments during the assessment process.

Access arrangements
Access arrangements (including modified papers) are the principal way in which Cambridge International complies with our duty, as guided by the UK Equality Act (2010), to make ‘reasonable adjustments’ for candidates with special educational needs (SEN), disability, illness or injury. Where a candidate would otherwise be at a substantial disadvantage in comparison to a candidate with no SEN, disability, illness or injury, we may be able to agree pre-examination access arrangements. These arrangements help a candidate by minimising accessibility barriers and maximising their opportunity to demonstrate their knowledge, skills and understanding in an assessment.
Important:

- Requested access arrangements should be based on evidence of the candidate’s barrier to assessment and should also reflect their normal way of working at school; this is in line with the Cambridge Handbook www.cambridgeinternational.org/eoguide
- For Cambridge International to approve an access arrangement, we will need to agree that it constitutes a reasonable adjustment, involves reasonable cost and timeframe and does not affect the security and integrity of the assessment.
- Availability of access arrangements should be checked by centres at the start of the course. Details of our standard access arrangements and modified question papers are available in the Cambridge Handbook www.cambridgeinternational.org/eoguide
- Please contact us at the start of the course to find out if we are able to approve an arrangement that is not included in the list of standard access arrangements.
- Candidates who cannot access parts of the assessment may be able to receive an award based on the parts they have completed.

After the exam

Grading and reporting

Grades A*, A, B, C, D or E indicate the standard a candidate achieved at Cambridge O Level.

A* is the highest and E is the lowest. ‘Ungraded’ means that the candidate’s performance did not meet the standard required for grade E. ‘Ungraded’ is reported on the statement of results but not on the certificate.

In specific circumstances your candidates may see one of the following letters on their statement of results:

- Q (PENDING)
- X (NO RESULT).

These letters do not appear on the certificate.

On the statement of results and certificates, Cambridge O Level is shown as GENERAL CERTIFICATE OF EDUCATION (GCE O LEVEL).

How students and teachers can use the grades

Assessment at Cambridge O Level has two purposes:

1. to measure learning and achievement
   - The assessment confirms achievement and performance in relation to the knowledge, understanding and skills specified in the syllabus, to the levels described in the grade descriptions.
2. to show likely future success
   - The outcomes help predict which students are well prepared for a particular course or career and/or which students are more likely to be successful.
   - The outcomes help students choose the most suitable course or career.
Grade descriptions

Grade descriptions are provided to give an indication of the standards of achievement candidates awarded particular grades are likely to show. Weakness in one aspect of the examination may be balanced by a better performance in some other aspect.

Grade descriptions for Cambridge O Level Mathematics (Syllabus D) will be published after the first assessment of the syllabus in 2025.
Changes to this syllabus for 2025, 2026 and 2027

The syllabus has been reviewed and revised for first examination in 2025.

You must read the whole syllabus before planning your teaching programme.

Changes to syllabus content

- The wording of learning outcomes has been updated and additional notes and examples included, to clarify the depth of teaching.
- The subject content has also been refreshed and updated, with some topics and learning outcomes added and some removed. Significant changes to content have been summarised below.
- New topics added:
  - 1.17 Exponential growth and decay
  - 1.18 Surds
- Topics removed:
  - Loci
  - Matrices
- New content included within existing topics (number in brackets is the topic number according to this updated syllabus):
  - reciprocals (1.1)
  - recurring decimals (1.4)
  - expanding algebraic expressions with products of more than two brackets (2.2)
  - factorising expressions in the form \(ax^3 + bx^2 + cx\) (2.2)
  - conventions for representing inequalities on a number line and graphically (2.6)
  - interpreting the gradients of curves (2.9)
  - graphs of functions in the form \(ax^n\) now include \(n\) values of \(-\frac{1}{2}\) and \(\frac{1}{2}\) (2.10)
  - graphs of functions in the form \(ab^x\) now include a constant, \(c\), i.e. \(ab^x + c\) (2.10)
  - drawing and interpreting graphs representing exponential growth and decay problems (2.10)
  - recognising, sketching and interpreting graphs of specified functions, including knowledge of turning points, asymptotes and symmetry where applicable (2.11)
  - domain and range (2.12)
  - composite functions (2.12)
  - terms frustum, hemisphere, radii, semicircle, major and minor (4.1)
  - alternate segment theorem (4.7)
  - calculating the angle between a line and a plane (6.4)

continued
Changes to syllabus content (continued)

- Learning outcomes removed from existing topics (topic number in brackets reflect the numbering in this updated syllabus):
  - proper subsets (1.2)
  - increasing and decreasing a quantity by a given ratio (1.11)
  - reading dials (1.15)
  - use of maps to notation, e.g. \( f: x \mapsto y \) (2.12)
  - constructing simple geometric shapes that cannot be formed only from triangles (4.2)
  - constructing perpendicular bisectors (4.2)
  - constructing angle bisectors (4.2)
  - showing that two triangles are congruent (4.4)
  - the hat notation over angles has been removed, e.g. \( \hat{PQR} = 37^\circ \).

- The teaching time has not changed.
- Mathematical notation is now included within the subject content.
- The learning outcomes in the subject content have been numbered, rather than listed by bullet points.
- The Details of the assessment section now includes:
  - the List of formulas that are provided in the examinations
  - mathematical conventions.
- A list of command words used in the assessments has been included.
- The wording of the learner attributes have been updated to improve the clarity of wording.
- The wording of the aims have been updated to improve the clarity of wording but the meaning is the same.
- The wording of the assessment objectives (AOs) has been updated. There are no changes to the knowledge and skills being assessed for each AO.

Changes to assessment (including changes to specimen papers)

- The examination papers have been rebalanced to provide improved accessibility and a better candidate experience.
- Both examination papers will include a List of formulas on page 2.
- Mark schemes have been updated to award more marks for working where appropriate, in alignment with other Cambridge Mathematics qualifications.
- Changes to Paper 1 Non-calculator:
  - number of marks increased to 100 marks
  - includes a mixture of structured and unstructured questions.
- The duration of Paper 1 has not changed, it is still 2 hours.
- Changes to Paper 2 Calculator:
  - duration decreased to 2 hours
  - includes a mixture of structured and unstructured questions.
- The number of marks in Paper 2 has not changed, it is still 100 marks.
In addition to reading the syllabus, you should refer to the updated specimen assessment materials. The specimen papers will help your students become familiar with exam requirements and command words in questions. The specimen mark schemes explain how students should answer questions to meet the assessment objectives.

Any textbooks endorsed to support the syllabus for examination from 2025 are suitable for use with this syllabus.