## Cambridge Pre-U

## MATHEMATICS

9794/02
Paper 2 Pure Mathematics 2
For examination from 2020
SPECIMEN PAPER 2 hours

You must answer on the answer booklet/paper.

You will need: Answer booklet/paper
Graph paper
List of formulae (MF20)

## INSTRUCTIONS

- Answer all questions.
- Follow the instructions on the front cover of the answer booklet. If you need additional answer paper, ask the invigilator for a continuation booklet.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question


## INFORMATION

- The total mark for this paper is 80 .
- The number of marks for each question or part question is shown in brackets [ ].

1 (a) Express each of the following as a single logarithm.
(i) $\log _{a} 5+\log _{a} 3$
(ii) $5 \log _{b} 2-3 \log _{b} 4$
(b) Express $\left(9 a^{4}\right)^{-\frac{1}{2}}$ as an algebraic fraction in its simplest form.
(c) Show that $\frac{3 \sqrt{3}-1}{2 \sqrt{3}-3}=\frac{15+7 \sqrt{3}}{3}$.


The diagram shows a triangle $A B C$ in which angle $C=30^{\circ}, B C=x \mathrm{~cm}$ and $A C=(x+2) \mathrm{cm}$. Given that the area of triangle $A B C$ is $12 \mathrm{~cm}^{2}$, calculate the value of $x$.

3 (a) The points $A$ and $B$ have coordinates $(-4,4)$ and $(8,1)$ respectively. Find the equation of the line $A B$. Give your answer in the form $y=m x+c$.
(b) Determine, with a reason, whether the line $y=7-4 x$ is perpendicular to the line $A B$.

4 (a) Show that $2 x^{2}-10 x-3$ may be expressed in the form $a(x+b)^{2}+c$ where $a, b$ and $c$ are real numbers to be found. Hence write down the coordinates of the minimum point on the curve.
(b) Solve the equation $4 x^{4}-13 x^{2}+9=0$.


The diagram shows a sector of a circle, $O M N$. The angle $M O N$ is $2 x$ radians, the radius of the circle is $r$ and $O$ is the centre.
(a) Find expressions, in terms of $r$ and $x$, for the area, $A$, and the perimeter, $P$, of the sector.
(b) Given that $P=20$, show that $A=\left(\frac{10}{1+x}\right)^{2}$.
(c) Find $\frac{\mathrm{d} A}{\mathrm{~d} x}$, and hence find the value of $x$ for which the area of the sector is a maximum.

6 Diane is given an injection that combines two drugs, Antiflu and Coldcure. At time $t$ hours after the injection, the concentration of Antiflu in Diane's bloodstream is $3 \mathrm{e}^{-0.02 t}$ units and the concentration of Coldcure is $5 \mathrm{e}^{-0.07 t}$ units. Each drug becomes ineffective when its concentration falls below 1 unit.
(a) Show that Coldcure becomes ineffective before Antiflu.
(b) Sketch, on the same diagram, the graphs of concentration against time for each drug.
(c) 20 hours after the first injection, Diane is given a second injection. Determine the concentration of Coldcure 10 hours later.

7 Solve the differential equation $x^{2} \frac{\mathrm{~d} y}{\mathrm{~d} x}=\sec y$ given that $y=\frac{\pi}{6}$ when $x=4$ giving your answer in the form $y=\mathrm{f}(x)$.

8 The parametric equations of a curve are

$$
x=\mathrm{e}^{2 t}-5 t, \quad y=\mathrm{e}^{2 t}-3 t .
$$

(a) Find $\frac{\mathrm{d} y}{\mathrm{~d} x}$ in terms of $t$.
(b) Find the equation of the tangent to the curve at the point when $t=0$, giving your answer in the form $a y+b x+c=0$ where $a, b$ and $c$ are integers.

9 The points $A$ and $B$ have position vectors $\mathbf{a}$ and $\mathbf{b}$ relative to an origin $O$, where $\mathbf{a}=5 \mathbf{i}+4 \mathbf{j}-2 \mathbf{k}$ and $\mathbf{b}=-7 \mathbf{i}+3 \mathbf{j}+\mathbf{k}$.
(a) Find the length of $A B$.
(b) Use a scalar product to find angle $O A B$.

10 A curve has equation

$$
y=\mathrm{e}^{a x} \cos b x
$$

where $a$ and $b$ are constants.
(a) Show that, at any stationary points on the curve, $\tan b x=\frac{a}{b}$.
(b)


Values of related quantities $x$ and $y$ were measured in an experiment and plotted on a graph of $y$ against $x$, as shown in the diagram. Two of the points, labelled $A$ and $B$, have coordinates $(0,1)$ and $(0.2,-0.8)$ respectively. A third point labelled $C$ has coordinates $(0.3,0.04)$. Attempts were then made to find the equation of a curve which fitted closely to these three points, and two models were proposed.

In the first model the equation is $y=\mathrm{e}^{-x} \cos 15 x$.
In the second model the equation is $y=f \cos (\lambda x)+g$, where the constants $f, \lambda$, and $g$ are chosen to give a maximum precisely at the point $A(0,1)$ and a minimum precisely at the point $B(0.2,-0.8)$.

By calculating suitable values evaluate the suitability of the two models.

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